that the steady-state deuterium atom concentration depends on deuterium pressure as shown in the upper part of Fig. 6. Over the range of deuterium pressure covered, $G(\mathrm{HD})$ is essentially proportional to [D] so that the similarity of the curves of $G(\mathrm{HD})$ and [D] (Fig. 1 and 6) demonstrate the self-consistency of the treatment in regard to saturation of $G(\mathrm{HD})$.

For the second point it is easily shown from a steadystate treatment for $\mathrm{CH}_{2}$ D radicals that

$$
\frac{\left[\mathrm{CH}_{3}\right]}{\left[\mathrm{CH}_{2} \mathrm{D}\right]}=\frac{4}{3}\left[\frac{1}{2}+\frac{k_{3}[\mathrm{M}]}{k_{\mathrm{d}}}+\frac{2 k_{8}^{1 / 2} R^{\circ}{ }_{\mathrm{C} 2 \mathrm{C}_{8}}{ }^{1 / 2}}{k_{2}[\mathrm{D}]}\left(1+\frac{k_{3}[\mathrm{M}]}{k_{\mathrm{d}}}\right)\right]
$$

(E18)
Using E18 and E8 and our values for the pertinent rate constants, we have calculated the lower curve in Fig. 6 for the ratio $\left[\mathrm{CH}_{2} \mathrm{D}\right] /\left[\mathrm{CH}_{3}\right]$. The agreement of the experimental points, particularly above 100 mm . where the treatment is expected to be more valid and where experimental error in determining the product $\mathrm{CH}_{2} \mathrm{D}_{2}$ is lessened, is evidence of the self-consistency of our treatment.

As a final check on the validity of our assumed mechanism we now consider the isotopic distribution of ethanes. As mentioned previously, we carried out a mass spectral analysis, using parent peaks, of the deuterated ethanes for the irradiations at 150 mm . of deuterium. Only analyses above ethane- $d_{0}$ are considered at all accurate because of sizable contributions from deuterated propane, the net result of which is to make the ethane $d_{0}$ value too small. The mass spectrometrically determined values normalized to unity

Table I

|  | Isotopic Ethane Distribution |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :---: | :---: |
| Species | Calcd. | Obsd. | Species | Calcd. | Obsd. |  |  |
| $\mathrm{C}_{2} \mathrm{H}_{8}$ | 3.4 | 0.7 | $\mathrm{C}_{2} \mathrm{H}_{2} \mathrm{D}_{4}$ | 0.34 | 0.40 |  |  |
| $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{D}$ | 2.1 | 2.0 | $\mathrm{C}_{2} \mathrm{HD}_{5}$ | .12 | 0.09 |  |  |
| $\mathrm{C}_{2} \mathrm{H}_{4} \mathrm{D}_{2}$ | 2.0 | 1.5 | $\mathrm{C}_{2} \mathrm{D}_{5}$ | .02 | $\ldots$ |  |  |
| $\mathrm{C}_{2} \mathrm{H}_{8} \mathrm{D}_{4}$ | 1.0 | 1.0 |  |  |  |  |  |

at ethane $-d_{3}$ are shown in column 3 of Table I. In column 2 of Table I, also normalized to unity at ethane- $d_{3}$, are values calculated using $\geq$ q. E $8-$ E10, the assumption that all ethane arises by methyl recombination, and the assumption that the recombination rate constant for like radicals is one-half that for unlike. We consider the degree of agreement, for deuteration above $d_{0}$, to be evidence of the validity of our mechanism.

We are somewhat at a loss to explain the discrepancies between this work and that of Firestone, et al. ${ }^{8}$ These authors, working at much higher deuterium pressures, found no ethane, so that we are limited in using our eq. E18 to calculate the theoretical $G\left(\mathrm{CH}_{3} \mathrm{D}\right) / G$ $\left(\mathrm{CH}_{2} \mathrm{D}_{2}\right)$. If we use their estimated upper limit to ethane formation and their estimate of the steady-state deuterium atom concentration in eq. E18, we calculate that they should have observed a minimum value of 0.23 for $G\left(\mathrm{CH}_{2} \mathrm{D}_{2}\right) / G\left(\mathrm{CH}_{3} \mathrm{D}\right)$. As this should have been within their capability of detection, the much higher pressure of deuterium cannot be the explanation. The only explanation left to us at the moment is that Firestone, et al., ${ }^{8}$ used no ionic scavenger and that hence a major part of their exchange may be due to ionic intermediates. The ionic paths, which are presumably absent in our work, lead by reasonable mechanistic schemes only to $\mathrm{CH}_{3} \mathrm{D}$ as a primary product.

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# The Crystal Structure of Bis-( $m$-chlorobenzoyl)-methane ${ }^{12}$ 

By Gordon R. Engebretson and R. E. Rundle ${ }^{1 b}$<br>Received April 17, 1963


#### Abstract

The crystal structure of bis-( $m$-chlorobenzoyl)-methane has been determined by three-dimensional anisotropic least squares refinement of scintillation counter data. The molecule was found to be nearly planar with a maximum deviation from the least squares molecular plane of $0.068 \AA$. and an average deviation of $0.023 \AA$. Fourier transform techniques to locate phenyl rings provided the key to the structure determination. The intramolecular bond distances and thermal parameters of the oxygen atoms support a resonant, enol ring with a symmetric, intramolecular hydrogen bond. The structure confirms conclusions from the structure of bis- $(m$ -bromobenzoyl)-methane where the symmetry of the molecule was forced by the crystal symmetry.


## Introduction

Interest in short, strong, intramolecular hydrogen bonds has prompted structural investigations of $\beta$ diketones and other intramolecular, hydrogen-bonded compounds. It has been established that the $\beta$ diketones exist almost completely in the enol form, but the question has been whether the structure is a statistical distribution of the two enol forms

or a symmetric resonance hybrid of the two.

In the one previous structural investigation of $\beta$ diketones the hydrogen atom was required to lie on a symmetry element. ${ }^{2}$ There is the possibility, in such a case, that the observed symmetry results from averaging the results of two orientations of somewhat asymmetric molecules. The present investigation was undertaken to see if the apparent symmetry of a $\beta$ diketone persists in an asymmetric, crystalline environment.

Preparation and Properties of the Crystals.-Crystals of bis-m-(chlorobenzoyl)-methane were prepared

[^0](2) D. Williams, R. Rundle, and W. Dumke. Acta Cryst., 15, 627 (1962):


Fig. 1.-Weighted reciprocal lattice of the (h0l) zone of bis( $m$-chlorobenzoyl)-methane.
by a basic condensation of $m$-chloroethyl benzoate and $m$-chloroacetophenone in the presence of sodium amide. ${ }^{3}$ Clear orthorhombic needles (m.p. 154-155 ${ }^{\circ}$ ) were obtained by recrystallization from chloroform. These had a density of $1.50 \mathrm{~g} . / \mathrm{cc}$. as determined by the flotation method.

X-Ray diagrams confirmed the orthorhombic symmetry. From back-reflection, Weissenberg, diffraction patterns lattice constants were obtained: $a=30.082 \pm$ $0.002, b=3.850 \pm 0.005, c=11.123 \pm 0.002 \AA$. The observed lattice constants and density require four molecules in a primitive, rhombic cell.

Systematic absences on diffraction patterns are $\{0 k l\}$ if $l=2 n+1$ and $\{h 0 l\}$ if $h=2 n+1$, suggesting space groups Pcam or Pca2. . The fourfold positions in the former are special positions, either at centers of symmetry, which would require an impossible linear $\mathrm{C}-\mathrm{C}-\mathrm{C}$ bonding at the center of the molecule, or on mirror planes at $Z=1 / 4,3 / 4$.

If the molecules were to lie on the mirror planes the short axis, $3.85 \AA$., would have to accommodate the width of the molecule, which is not possible. If two halves of the molecule were related by a mirror plane the packing would become" poor for this shape of unit cell. These considerations seem to require the space group $\mathrm{Pca} 2_{1}$, which the final structure confirms.

Intensity Data.-X-Ray intensity data were obtained using nickel-filtered, copper $\mathrm{K} \alpha$ radiation, a G.E. single crystal orienter, scintillation counter, and $\theta-2 \theta$ scan technique. The crystal used had a trapezoidal cross section with maximum dimensions of such size, 96.7 and $115 \mu$, that absorption corrections were necessary. These were made by carefully measuring the crystal and employing a program, ABCOR-I, ${ }^{4 a}$ and the Iowa State Cyclone computer to make these corrections after the method of Busing and Levy. ${ }^{4 b}$

Unobserved reflections were assigned a most probable intensity and error depending upon the minimum observable intensity at the specified lattice point. ${ }^{5}$ The errors of the intensities of the observed reflections were obtained from the statistical counting errors in peak and background, analysis of errors from the reproducibility of standard reflections with time, estimated error

[^1]

Fig. 2.-Fourier transform for the bis-( $m$-chlorobenzoyl)methane molecule with the length of the molecule tilted $13^{\circ}$ to the real space $x$-axis and the molecule tilted $24^{\circ}$ out of the (010) plane. Circle is the "benzene circle."


Fig. 3.-Final Fourier projected onto (010). Dashed line is $1 \mathrm{e}^{-} / \AA \mathrm{A}^{2}$ contour. Other contours $\mathrm{e}^{-} / \AA^{2}{ }^{2}$
in streak corrections, etc. The weighting of reflections in least squares refinements was then $W_{\mathrm{h}}=1 / \sigma_{\mathrm{h}}{ }^{2}$ where $W$ is the weighting factor and $\sigma_{\mathrm{h}}{ }^{2}$ is the error in intensity for reflection $(h)$.

Structural Investigations.-The Patterson projection onto (010) was calculated, but it was not readily interpretable, since the chlorine atom did not serve as a heavy atom in this structure.

It was then decided to calculate a Fourier transform, making use of the phenyl rings in the molecule to find the angular orientation of the molecule in the unit cell. A weighted reciprocal lattice was constructed using the $\{h 0 l\}$ data (Fig. 1). The circle indicated is the benzene circle, i.e., the locus to which a benzene ring would transform. A study of the weighted reciprocal lattice showed twelve peaks on or near the benzene circle. Since there are four molecules in the unit cell which are parallel in projection in groups of two, one would expect two distinct angular orientations of the benzene rings, and hence twelve different peaks on the benzene circle. The peaks off the benzene circle near the $c^{*}$-axis indicated that the rings were rotated out of the plane of the benzene circle about an axis perpendicular to the line from the origin to the peaks. A measure of the amount of shift of the peaks off the benzene circle led to an out-of-plane tilt of $24^{\circ}$. The other peaks on the benzene circle near the $a^{*}$ axis led to an in-plane rotation of the benzene rings of $13^{\circ}$. Figure 2 shows the Fourier transform for one molecule using the indicated angles (the origin peak has been omitted for clarity). A re-examination of the twodimensional Patterson projection using this information led to a satisfactory trial structure.


Fig. 4.-Molecular environment of a molecule of bis-( $m$-chlorobenzoyl)-methane projected onto the (010) plane with space group symmetry elements indicated.




Fig. 5.-Anisotropic thermal stereograms for selected atoms in the bis-(m-chlorobenzoyl)-methane molecule. The plane of the paper is the molecular least squares plane and the stereograms are oriented in the same manner as the molecule at the bottom of the figure. The orientation of the reference coordinate system is also shown.

The IBM 704 least squares program of Busing and Levy ${ }^{6}$ (1959) was used to obtain a least squares refinement of the $\{h 01\}$ data, leading to an $R$-value of $5.6 \%$.
(6) W. Busing and H. A. Levy. U.S.A.E.C. Report. ORNL 59-4-37 (1959).

A three-dimensional Patterson map was calculated and a trial structure was found based on this map and the Fourier transform alone.

Refinement proceeded through several cycles of least squares using isotropic temperature factors for each

Table I
Final Positional and Anisotropic Thermal Parameters and Their Standard Deviations $\times 10^{5}$

| Atom | $x / a$ | $y / b$ | z/c | $\beta_{11}$ | $\beta_{22}$ | $\beta_{33}$ | $\beta_{12}$ | $\beta_{18}$ | $\beta_{28}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Cl}_{1}$ | 40885 | 4084 | 0 | 88 | 9627 | 879 | -25 | -95 | $-139$ |
|  | 7 | 70 | 0 | 2 | 206 | 18 | 18 | 6 | 71 |
| $\mathrm{Cl}_{2}$ | 83345 | 20930 | 21959 | 73 | 11668 | 1463 | 45 | 36 | 134 |
|  | 6 | 89 | 36 | 2 | 265 | 30 | 21 | 7 | 87 |
| $\mathrm{O}_{1}$ | 58081 | 2356 | 1947 | 114 | 12100 | 658 | 82 | -7 | -1152 |
|  | 17 | 200 | 53 | 7 | 658 | 57 | 66 | 16 | 171 |
| $\mathrm{O}_{2}$ | 66147 | 4761 | 6265 | 92 | 12585 | 721 | 49 | 15 | -932 |
|  | 19 | 213 | 54 | 6 | 734 | 53 | 61 | 15 | 186 |
| Cl | 44940 | 18084 | 9929 | 82 | 7955 | 722 | 70 | -14 | 117 |
|  | 25 | 273 | 77 | 8 | 845 | 73 | 68 | 20 | 223 |
| C 2 | 49365 | 12686 | 7181 | 89 | 7212 | 766 | 63 | -42 | 796 |
|  | 25 | 228 | 77 | 8 | 716 | 76 | 63 | 21 | 205 |
| C3 | 52581 | 23767 | 15393 | 94 | 6680 | 544 | -21 | -14 | 384 |
|  | 25 | 254 | 75 | 8 | 669 | 56 | 66 | 17 | 183 |
| Ct | 51325 | 39178 | 26211 | 97 | 8237 | 683 | -61 | $-20$ | -344 |
|  | 25 | 238 | 83 | 9 | 778 | 64 | 66 | 21 | 217 |
| Cs | 46833 | 44041 | 28823 | 97 | 9158 | 773 | -7 | -7 | -81 |
|  | 26 | 274 | 86 | 9 | 843 | 79 | 76 | 23 | 230 |
| C6 | 43521 | 32426 | 20746 | 75 | 8376 | 845 | 74 | 29 | -38 |
|  | 23 | 247 | 92 | 7 | 723 | 69 | 60 | 21 | 218 |
| $\mathrm{C}_{7}$ | 57333 | 17847 | 12125 | 95 | 7256 | 569 | 9 | 3 | -6 |
|  | 25 | 260 | 75 | 9 | 726 | 59 | 66 | 20 | 186 |
| Cs | 60838 | 27812 | 19686 | 64 | 8699 | 585 | 28 | 7 | 184 |
|  | 21 | 258 | 75 | 6 | 712 | 64 | 62 | 17 | 198 |
| $\mathrm{C}_{8}$ | 65235 | 21088 | 16382 | 88 | 6074 | 614 | 150 | $-12$ | 98 |
|  | 23 | 233 | 71 | 7 | 643 | 59 | 62 | 17 | 181 |
| Cl 10 | 76557 | 48437 | 37647 | 116 | 832 | 791 | -94 | -67 | 211 |
|  | 28 | 280 | 86 | 11 | 800 | 75 | 82 | 24 | 225 |
| Cl | 72238 | 55477 | 41867 | 83 | 9589 | -113 | -6 | -6 | 535 |
|  | 25 | 283 | 83 | 8 | 849 | 77 | 73 | 22 | 231 |
| $\mathrm{Cl}_{12}$ | 68564 | 46246 | 34855 | 98 | 8183 | 702 | -21 | 22 | -71 |
|  | 27 | 264 | 77 | 9 | 740 | 67 | 77 | 21 | 208 |
| $\mathrm{C}_{18}$ | 61256 | 30733 | 23842 | 73 | 8016 | 559 | -33 | -5 | 325 |
|  | 22 | 225 | 67 | 7 | 692 | 61 | 62 | 18 | 175 |
| Cl 4 | 73303 | 22839 | 20002 | 88 | 8992 | 781 | -55 | -33 | 416 |
|  | 23 | 275 | 88 | 7 | 787 | 74 | 70 | 21 | 236 |
| Cls | 76998 | 31868 | 27006 | 67 | 8293 | 1096 | 66 | 26 | 491 |
|  | 25 | 273 | 94 | 7 | 776 | 97 | 67 | 22 | 258 |
| $\mathrm{H}_{2}$ | 50300 | $-500$ | $-1000$ | 138 | 8433 | 1010 |  |  |  |
| $\mathrm{H}_{4}$ | 55600 | 47000 | 32500 | 138 | 8433 | 1010 |  |  |  |
| $\mathrm{H}_{5}$ | 46000 | 55100 | 36800 | 138 | 8433 | 1010 |  |  |  |
| H8 | 39200 | 34300 | 22900 | 138 | 8433 | 1010 |  |  |  |
| $\mathrm{H}_{8}$ | 60200 | 40300 | 28003 | 138 | 8433 | 1010 |  |  |  |
| $\mathrm{H}_{10}$ | 79700 | 55400 | 42500 | 138 | 8433 | 1010 |  |  |  |
| $\mathrm{H}_{1}$ | 71800 | 67500 | 50400 | 138 | 8433 | 1010 |  |  |  |
| $\mathrm{H}_{12}$ | 65300 | 50800 | 39700 | 138 | 8433 | 1010 |  |  |  |
| $\mathrm{H}_{14}$ | 73700 | 9900 | 11700 | 138 | 8433 | 1010 |  |  |  |
| ( $\mathrm{H}_{2}$ is bonded to $\mathrm{C}_{2}$, etc.) |  |  |  |  |  |  |  |  |  |

independent atom to $R=13.8 \%$, then to refinement cycles using anisotropic temperature factors using Busing and Levy's least squares program, ORXLS. ${ }^{6}$ Near the end of the refinement two rejection tests were made. The first gave zero weight in the refinement to unobserved reflections where $F_{\mathrm{c}}<F_{\mathrm{o}}$ and where $F_{\mathrm{o}}$ had been assigned a value by Hamilton's method. ${ }^{5}$ The second test gave zero weight to reflections where $\left|F_{0}-F_{\mathrm{c}}\right| / \sigma\left(F_{\mathrm{o}}\right)>6$. Fourteen reflections of this type were found. In every case $F_{\mathrm{c}}$ was greater than $F_{\mathrm{o}}$, and a remeasurement of these reflections showed that an error had been made, presumably in hand setting counter and/or crystal angles for the measurement. Remeasured structure factors were reinserted into the final refinement cycles. Toward the end, all the hydrogens but the enolic hydrogen were inserted assuming $\mathrm{C}-\mathrm{H}=1.07 \AA$. and using estimated temperature factors for hydrogen atoms. Certain carbon positions changed by more than one standard deviation in the next cycle, so new, consistent, hydrogen positions were reinserted. (Hydrogen parameters were held constant during least squares refinement.) The final $R$-value was $5.8 \%$ for observed data, $10.2 \%$ over all, and $\left[\Sigma W\left(F_{\mathrm{o}}-F_{\mathrm{c}}\right)^{2} /(m-n)\right]^{1 / 2}=1.86$, indicating a reasonable weighting scheme.

Since for some of the most intense reflections extinction seems to be $5 \%$ or less, extinction effects were ignored in the refinement.

Figure 3 shows the final Fourier projection onto (010). For atomic designations see Fig. 5 .

Table I lists the final positional and anisotropis thermal parameters with their respective standard errors for bis- ( $m$-chlorobenzoyl)-methane.

Table II lists a comparisin of the observed and calculated structure factors based on the parameters listed in Table I.

## Discussion of the Structure

The molecules were found to be nearly parallel to the (010) plane. The chlorine atoms tend to pack in zig-zag chains in the $y$-direction. It can be seen that the two nonequivalent chlorine atoms have different atomic environments. One chlorine atom "sees" the oxygen side of the carbonyl groups while the other chlorine atom "sees" the carbon side of the carbonyl groups.

Least squares planes were calculated for the entire molecule and several subgroups within the molecule. The IBM 650 program of Stewart (1960) was used. Least squares planes were calculated for the $\mathrm{Cl}_{1}$ atom and its attached phenyl group (plane 1), $\mathrm{Cl}_{2}$ and its attached phenyl group (plane 2), the enol subgroup (plane 3), and the entire molecule (plane 4). The planes were of the form

$$
A x+B y+C z+1=0
$$

The coefficients are listed in Table III.
The molecule was found to be planar with a maximum deviation of $0.068 \AA$. from the plane and an average deviation of $0.023 \AA$. The distance of each atom (excluding the hydrogen atoms) from the molecular least squares plane is listed in Table IV.

The $\mathrm{C}-\mathrm{C}$ bond distances in the benzene rings were near the accepted experimental value of $1.397 \AA$. except for two shorter bonds between $\mathrm{C}_{13}-\mathrm{C}_{14}$ and $\mathrm{C}_{10}-\mathrm{C}_{15}$. The average $\mathrm{C}-\mathrm{C}$ bond distances for the two phenyl rings were 1.395 and $1.382 \AA$, the latter ring containing the two short bonds. (We presume these two short bonds are the result of some systematic error.) The bond distances between $\mathrm{C}_{3}-\mathrm{C}_{7}$ and $\mathrm{C}_{9}-$ $\mathrm{C}_{13}$ (1.492 and $1.482 \AA$.) are typical of $\mathrm{C}-\mathrm{C}$ single bonds trigonally coordinated. In the enol ring the distances between $\mathrm{C}_{7}-\mathrm{C}_{8}$ and $\mathrm{C}_{8}-\mathrm{C}_{9}(1.399 \AA$.$) are$ indicative of $50 \%$ double bond character. This supports the hypothesis that these bond distances are determined by resonance between the two enol forms. The two CO bonds ( $1.31 \AA$.) are longer than typical CO double bonds ( $1.23 \AA$.), shorter than typical single CO bonds ( $1.43 \AA$.), and rather closer to the former, again supporting resonance in the enol ring. Table V compares the intramolecular bond distances and errors within a molecule of bis-( $m$-chlorobenzoyl)methane to the equivalent distances in bis- ( $m$-bromo-benzoyl)-methane. ${ }^{2}$ Similarly, Table VI compares bond angles between the two derivatives.

No significant deviations from symmetry can be detected in the $m$-chloro derivative, nor do there appear to be any significant differences between $m$ bromo and $m$-chloro derivatives except in ${\angle \mathrm{C}_{3} \mathrm{C}_{7} \mathrm{C}_{8}}$ which is considerably larger in the bromo derivative. The reason for this is not clear. (The $99 \%$ confidence level is three times the standard deviations quoted.)

The largest thermal amplitudes of the oxygen atoms are normal to the $\mathrm{C}-\mathrm{O}$ bond and hence did not affect the accuracy of this bond distance seriously. The average chlorine-carbon distance of $1.729 \AA$. agrees quite well with that observed for o-dichlorobenzene (1.735 $\AA.)^{7}$ but is longer than the average accepted distance. ${ }^{8}$
(7) L. O. Brockway and K. J. Palmer. J. Am. Chem. Soc.. 59, 2181 (1937)
(8) "Tables of Interatomic Distances." L. E. Sutton. Ed.. The Chemica 1 Society. London. 1958.

Table II
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 | 39 |
| :--- |
| 38 |
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$\therefore$ －



Table III
Least SQuares Plane Coefficients for Bis-( $m$-chlorobenzoyl)-methane

| Plane | $A$ | $B$ | $C$ |
| :---: | :---: | :---: | ---: |
| 1 | -0.05307 | -2.09875 | 1.02959 |
| 2 | -.05034 | -0.99214 | 0.50857 |
| 3 | -.05874 | -0.92279 | .49278 |
| 4 | -.06002 | -1.41053 | .71061 |

cosines of these axes for all the atoms. The reference coordinate system for these direction cosines is defined by the following: Axis I : the vector from $\mathrm{C}_{7}$ to $\mathrm{O}_{1}$. Axis II: the vector cross-product of Axis I into the vector from $\mathrm{C}_{7}$ to $\mathrm{C}_{8}$. Axis III: the vector cross-product of axis I into axis II. The anisotropic thermal stereograms for selected atoms are represented in Fig. 5. The length of each thermal axis is listed in $\AA$. The plane of the paper is the molecular least squares plane and
Table IV
Deviations of Atoms in $\AA$. from the Molecular Least SQutares Plane (Plane 4 of Table iti)

| Atom | $D,{ }^{\circ} \AA$. | Atom | D, ${ }^{\boldsymbol{a}} \AA$. | Atom | $D,{ }^{\text {a }} \AA$. | Atom | $D,{ }^{\circ} \AA$. | Atom | D. ${ }^{\text {a }}$ A. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Cl}_{1}$ | 0.0237 | $\mathrm{C}_{1}$ | -0.0165 | $\mathrm{C}_{5}$ | 0.0234 | $\mathrm{C}_{9}$ | -0.0256 | $\mathrm{C}_{13}$ | -0.0299 |
| $\mathrm{Cl}_{2}$ | . 0686 | $\mathrm{C}_{2}$ | . 0012 | $\mathrm{C}_{6}$ | . 0476 | $\mathrm{C}_{10}$ | -. 0206 | $\mathrm{C}_{15}$ | . 0100 |
| $\mathrm{O}_{1}$ | -. 0197 | $\mathrm{C}_{3}$ | -. 0199 | $\mathrm{C}_{7}$ | - . 0387 | $\mathrm{C}_{11}$ | -. 0038 | $\mathrm{C}_{15}$ | 0010 |
| $\mathrm{O}_{2}$ | . 0313 | $\mathrm{C}_{4}$ | . 0077 | $\mathrm{C}_{8}$ | - . 0461 | $\mathrm{C}_{12}$ | . 0061 |  |  |

${ }^{a}$ Distance from least squares plane.
Table V
A. Comparison of Intramolecular Bond Distances in

Bis-( $m$-chlorobenzoyl)-methane and
Bis-( $m$-BROMOBENZOYL)-METHANE ${ }^{a}$

| Bond | Distance |  | Bond | Distance, $\AA$. |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Cl}_{1}-\mathrm{C}_{1}$ | $1.731 \pm$ | . 008 | $\mathrm{Br}-\mathrm{C}_{1}$ | $1.901 \pm 0.007$ |  |
| $\mathrm{Cl}_{2}-\mathrm{C}_{15}$ | $1.727 \pm$ | . 008 \} |  |  |  |
| $\mathrm{O}_{2}-\mathrm{O}_{1}$ | $2.475 \pm$ | . 008 | $\mathrm{O}_{1}-\mathrm{O}_{1}{ }^{\prime}$ | $2.464 \pm$ | . 015 |
| $\mathrm{C}_{1}-\mathrm{C}_{8}$ | $1.391 \pm$ | . 012$\}$ | $\mathrm{C}_{1}-\mathrm{C}_{6}$ | $1.375 \pm$ | . 009 |
| $\mathrm{C}_{10}-\mathrm{C}_{15}$ | $1.351 \pm$ | . 014 \} |  |  |  |
| $\mathrm{C}_{6}-\mathrm{C}_{5}$ | $1.414 \pm$ | . 011$\}$ | $\mathrm{C}_{6}-\mathrm{C}_{5}$ | $1.397 \pm$ | . 010 |
| $\mathrm{C}_{10}-\mathrm{C}_{11}$ | $1.407 \pm$ | . 011 |  |  |  |
| $\mathrm{C}_{5}-\mathrm{C}_{4}$ | $1.395 \pm$ | . 010$\}$ | $\mathrm{C}_{5}-\mathrm{C}_{4}$ | $1.389 \pm$ | . 010 |
| $\mathrm{C}_{11}-\mathrm{C}_{12}$ | $1.398 \pm$ | . 010$\}$ |  |  |  |
| $\mathrm{C}_{4}-\mathrm{C}_{3}$ | $1.394 \pm$ | . 011$\}$ | $\mathrm{C}_{4}-\mathrm{C}_{3}$ | $1.410 \pm$ | . 008 |
| $\mathrm{C}_{12}-\mathrm{C}_{13}$ | $1.373 \pm$ | . 011$\}$ |  |  |  |
| $\mathrm{C}_{3}-\mathrm{C}_{2}$ | $1.381 \pm$ | . 010$\}$ | $\mathrm{C}_{3}-\mathrm{C}_{2}$ | $1.400 \pm$ | . 009 |
| $\mathrm{C}_{18}-\mathrm{C}_{14}$ | $1.362 \pm$ | . 010 \} |  |  |  |
| $\mathrm{C}_{1}-\mathrm{C}_{2}$ | $1.397 \pm$ | . 011$\}$ | $\mathrm{C}_{1}-\mathrm{C}_{2}$ | $1.392 \pm$ | 009 |
| $\mathrm{C}_{14}-\mathrm{C}_{15}$ | $1.401 \pm$ | . 010$\}$ |  |  |  |
| $\mathrm{C}_{3}-\mathrm{C}_{7}$ | $1.492 \pm$ | . 010$\}$ | $\mathrm{C}_{3}-\mathrm{C}_{7}$ | $1.457 \pm$ | 009 |
| $\mathrm{C}_{9}-\mathrm{C}_{19}$ | $1.482 \pm$ | . 010 |  |  |  |
| $\mathrm{C}_{7}-\mathrm{C}_{8}$ | $1.402 \pm$ | . 011$\}$ | $\mathrm{C}_{7}-\mathrm{C}_{8}$ | $1.393 \pm$ | . 008 |
| $\mathrm{C}_{8}-\mathrm{C}_{9}$ | $1.397 \pm$ | . 009 |  |  |  |
| $\mathrm{C}_{7}-\mathrm{O}_{1}$ | $1.299 \pm$ | . 010$\}$ | $\mathrm{C}_{7}-\mathrm{O}$ | $1.306 \pm$ | . 008 |
| $\mathrm{C}_{9}-\mathrm{O}_{2}$ | $1.318 \pm$ | . 009 |  |  |  |

${ }^{\text {a }}$ The bromo derivative has twofold symmetry in the molecule, hence only half of the atoms in the molecule are listed. Standard deviations in bond lengths are given.

The observed $\mathrm{O}-\mathrm{H}-\mathrm{O}$ distance of $2.475 \AA$. confirms the existence of a strong intramolecular hydrogen bond. The angles $\mathrm{C}_{7}-\mathrm{O}_{1}-\mathrm{O}_{2}$ and $\mathrm{C}_{9}-\mathrm{O}_{2}-\mathrm{O}_{1}$ are both less than $90^{\circ}$ and show that the two oxygen atoms are being forced apart somewhat by steric repulsions. If the hydrogen atom is placed on the line of centers of the two oxygen atoms, an improbably small $\mathrm{C}-\mathrm{O}-\mathrm{H}$ angle $\left(<90^{\circ}\right)$, at least $15^{\circ}$ less than normal, results. It seems likely that the hydrogen atom lies off the line of centers of the two oxygen atoms. Presumably the large out-of-plane thermal parameters of the oxygens are due to opposite displacements of the oxygens from the molecular plane as in the bromo derivative. ${ }^{2}$

The larger than normal angles $\mathrm{C}_{3}-\mathrm{C}_{7}-\mathrm{C}_{8}$ and $\mathrm{C}_{8}-$ $\mathrm{C}_{9}-\mathrm{C}_{13}$ indicate that these angles open to relieve the strain caused by the close approach of $\mathrm{H}_{8}$ to both $\mathrm{H}_{4}$ and $\mathrm{H}_{12}\left(\mathrm{H}_{4} \mathrm{H}_{8}\right.$ contact distance of $2.02 \AA ., \mathrm{H}_{12} \mathrm{H}_{8}$ contact distance of $1.95 \AA$.). This was also observed in the bromo derivative ( $\mathrm{H}_{4}{ }^{\prime} \mathrm{H}_{8}{ }^{\prime}$ distance of $2.01 \AA$.). (Hydrogen atoms are given the same number as the carbon to which they are bonded in Fig. 5.)

Table VII lists the lengths of the principal axes of the anisotropic thermal vibrations and the direction

Table VI
A Comparison of Bond Angles within Molecules of Bis-( $m$-chlorobenzoyl)-methane and Bis-( $m$-bromobenzoyl)-METHANE ${ }^{a}$

| Bis-( $m$-cblorobenzoyl)-methaneAtomsBond angle, deg. |  |  | Bis-(m-bromobenzoyl)-methane |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Atoms | Bond angle, |  |
| $\mathrm{Cl}_{1} \mathrm{C}_{1} \mathrm{C}_{6}$ | $117.3 \pm$ | . 6 | $\mathrm{BrC}_{1} \mathrm{C}_{8}$ | $119.5 \pm 0.6$ |  |
| $\mathrm{Cl}_{2} \mathrm{C}_{15} \mathrm{C}_{10}$ | $119.3 \pm$ |  |  |  |  |
| $\mathrm{Cl}_{2} \mathrm{C}_{1} \mathrm{C}_{2}$ | $119.4 \pm$ |  | $\mathrm{BrC}_{1} \mathrm{C}_{2}$ | $117.8 \pm$ |  |
| $\mathrm{Cl}_{2} \mathrm{C}_{15} \mathrm{C}_{14}$ | $118.9 \pm$ |  |  |  |  |
| $\mathrm{C}_{8} \mathrm{C}_{1} \mathrm{C}_{2}$ | $123.1 \pm$ |  | $\mathrm{C}_{8} \mathrm{C}_{1} \mathrm{C}_{2}$ | $122.7 \pm$ |  |
| $\mathrm{C}_{10} \mathrm{C}_{15} \mathrm{C}_{14}$ | $121.7 \pm$ |  |  |  |  |
| $\mathrm{C}_{1} \mathrm{C}_{8} \mathrm{C}_{5}$ | $117.3 \pm$ |  | $\mathrm{C}_{1} \mathrm{C}_{6} \mathrm{C}_{5}$ | $117.8 \pm$ | 7 |
| $\mathrm{C}_{15} \mathrm{C}_{10} \mathrm{C}_{11}$ | $118.3 \pm$ |  |  |  |  |
| $\mathrm{C}_{6} \mathrm{C}_{5} \mathrm{C}_{4}$ | $120.5 \pm$ |  | $\mathrm{C}_{8} \mathrm{C}_{6} \mathrm{C}_{4}$ | $121.6 \pm$ | . 6 |
| $\mathrm{C}_{10} \mathrm{C}_{11} \mathrm{C}_{12}$ | $119.6 \pm$ |  |  |  |  |
| $\mathrm{C}_{5} \mathrm{C}_{4} \mathrm{C}_{3}$ | $120.0 \pm$ | . 7 \} | $\mathrm{C}_{5} \mathrm{C}_{4} \mathrm{C}_{3}$ | $119.6 \pm$ | 7 |
| $\mathrm{C}_{11} \mathrm{C}_{12} \mathrm{C}_{13}$ | $120.7 \pm$ |  |  |  |  |
| $\mathrm{C}_{4} \mathrm{C}_{3} \mathrm{C}_{2}$ | $120.4 \pm$ |  | $\mathrm{C}_{4} \mathrm{C}_{3} \mathrm{C}_{2}$ | $119.2 \pm$ | 6 |
| $\mathrm{C}_{12} \mathrm{C}_{18} \mathrm{C}_{14}$ | $119.4 \pm$ |  |  |  |  |
| $\mathrm{C}_{8} \mathrm{C}_{2} \mathrm{C}_{1}$ | $118.4 \pm$ |  | $\mathrm{C}_{3} \mathrm{C}_{2} \mathrm{C}_{1}$ | $119.1 \pm$ | . 6 |
| $\mathrm{C}_{18} \mathrm{C}_{14} \mathrm{C}_{15}$ | $120.1 \pm$ |  |  |  |  |
| $\mathrm{C}_{4} \mathrm{C}_{3} \mathrm{C}_{7}$ | $122.3 \pm$ |  | $\mathrm{C}_{4} \mathrm{C}_{3} \mathrm{C}_{7}$ | $121.6 \pm$ | . 6 |
| $\mathrm{C}_{12} \mathrm{C}_{13} \mathrm{C}_{9}$ | $120.7 \pm$ |  |  |  |  |
| $\mathrm{C}_{2} \mathrm{C}_{3} \mathrm{C}_{7}$ | $117.2 \pm$ |  | $\mathrm{C}_{2} \mathrm{C}_{8} \mathrm{C}_{7}$ | $119.3 \pm$ | . 6 |
| $\mathrm{C}_{14} \mathrm{C}_{18} \mathrm{C}_{9}$ | $119.8 \pm$ |  |  |  |  |
| $\mathrm{C}_{3} \mathrm{C}_{7} \mathrm{C}_{8}$ | $122.2 \pm$ | . 7 \} | $\mathrm{C}_{3} \mathrm{C}_{7} \mathrm{C}_{8}$ | $125.0 \pm$ | . 6 |
| $\mathrm{C}_{18} \mathrm{C}_{9} \mathrm{C}_{8}$ | $123.6 \pm$ |  |  |  |  |
| $\mathrm{C}_{3} \mathrm{C}_{7} \mathrm{O}_{1}$ | $116.6 \pm$ |  | $\mathrm{C}_{3} \mathrm{C}_{7} \mathrm{O}$ | $115.6 \pm$ | 6 |
| $\mathrm{C}_{13} \mathrm{C}_{9} \mathrm{O}_{2}$ | $115.7 \pm$ |  |  |  |  |
| $\mathrm{O}_{1} \mathrm{C}_{7} \mathrm{C}_{8}$ | $121.2 \pm$ | . 6 \} | $\mathrm{OC}_{7} \mathrm{C}_{8}$ | $119.4 \pm$ | . 7 |
| $\mathrm{O}_{2} \mathrm{C}_{9} \mathrm{C}_{8}$ | $120.7 \pm$ | . 7 \} |  |  |  |
| $\mathrm{C}_{7} \mathrm{C}_{8} \mathrm{C}_{9}$ | $120.2 \pm$ | . 7 | $\mathrm{C}_{7} \mathrm{C}_{8} \mathrm{C}_{7}{ }^{\prime}$ | $122.2 \pm$ | 8 |
| $\mathrm{C}_{7} \mathrm{O}_{1} \mathrm{O}_{2}$ | $89.0 \pm$ | 7 7 | $\mathrm{C}_{7} \mathrm{OO}^{\prime}$ | $89.5 \pm$ | 8 |
| $\mathrm{C}_{9} \mathrm{O}_{2} \mathrm{O}_{1}$ | $88.8 \pm$ | . 6 |  |  |  |

${ }^{a}$ The central atom is the vertex. Standard deviations are given for bond angles.
the stereograms are in the same orientation as the molecule shown at the bottom of the figure. It is evident that the chlorine atoms have their shortest thermal amplitude nearly parallel to the $\mathrm{Cl}-\mathrm{C}$ bond and their largest amplitudes normal to this bond, as expected. The carbon atoms in the enol ring have their greatest thermal amplitude nearly perpendicular to the molecular least square plane. This is also true for the carbon atoms in the benzene rings. Hence it can be concluded that the molecule oscillates as a whole perpendicular to the molecular least squares plane. The two oxygen atoms have their lowest thermal amplitude nearly parallel to the $\mathrm{C}-\mathrm{O}$ bond. This gives some confidence to the hypothesis that the intramolecular hydrogen bond is the symmetrical type, for if it were not the thermal amplitude

| Atom | Principal axis | cos $\alpha$ | $\cos \beta$ | $\cos \gamma$ | Length, A. | Atom | Principal axis | $\cos \alpha$ | $\cos \beta$ | $\cos \gamma$ | Length, $\AA$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Cl}_{1}$ | 1 | -0.369 | 0.153 | -0.940 | 0.171 | $\mathrm{C}_{8}$ | 3 | 419 | 889 | 0.183 | 0.247 |
|  | 2 | - . 902 | . 192 | . 386 | 253 | $\mathrm{C}_{7}$ | 1 | -. 885 | 452 | -. 111 | 180 |
|  | 3 | 236 | 969 | . 069 | 268 |  | 2 | 139 | . 030 | -. 990 | 216 |
| $\mathrm{Cl}_{2}$ | 1 | -. 230 | . 051 | . 959 | . 181 |  | 3 | . 444 | . 891 | . 090 | 235 |
|  | 2 | . 013 | . 999 | -. 049 | 293 | $\mathrm{C}_{8}$ | 1 | . 024 | . 003 | $-1.000$ | 163 |
|  | 3 | 960 | . 001 | 280 | 302 |  | 2 | -. 812 | . 583 | -. 017 | 195 |
| $\mathrm{O}_{1}$ | 1 | 986 | . 082 | -. 143 | 174 |  | 3 | . 582 | 813 | . 016 | 259 |
|  | 2 | . 148 | . 059 | -. 987 | 231 | C9 | 1 | -. 006 | . 655 | -. 756 | 173 |
|  | 3 | - . 072 | . 995 | -. 071 | 315 |  | 2 | -. 956 | 219 | . 197 | 197 |
| $\mathrm{O}_{2}$ | 1 | -. 940 | . 124 | . 317 | 195 |  | 3 | . 294 | 723 | . 625 | 232 |
|  | 2 | -. 313 | . 054 | -. 948 | 203 | $\mathrm{C}_{10}$ | 1 | - . 553 | . 320 | -. 769 | 203 |
|  | 3 | . 135 | . 991 | . 012 | 323 |  | 2 | -. 155 | 868 | . 472 | 236 |
| $\mathrm{C}_{1}$ | 1 | -. 013 | . 274 | -. 962 | . 183 |  | 3 | . 818 | 381 | -. 431 | 259 |
|  | 2 | -. 843 | . 515 | . 158 | 215 | $\mathrm{C}_{11}$ | 1 | -. 145 | 267 | . 953 | 181 |
|  | 3 | . 538 | . 812 | . 224 | 268 |  | 2 | -. 589 | . 750 | -. 300 | 212 |
| $\mathrm{C}_{2}$ | 1 | -. 242 | 744 | -. 623 | . 168 |  | 3 | . 795 | . 605 | -. 048 | 287 |
|  | 2 | -. 287 | . 558 | . 779 | . 197 | $\mathrm{C}_{12}$ | 1 | -. 777 | . 359 | . 518 | 203 |
|  | 3 | -. 927 | . 367 | -. 079 | . 273 |  | 2 | -. 504 | . 139 | -. 852 | 223 |
| $\mathrm{C}_{3}$ | 1 | -. 601 | . 748 | -. 280 | . 175 |  | 3 | . 378 | . 923 | -. 073 | 237 |
|  | 2 | -. 085 | . 275 | . 956 | . 207 | $\mathrm{C}_{11}$ | 1 | -. 560 | . 524 | -. 642 | 173 |
|  | 3 | . 792 | . 604 | -. 089 | . 237 |  | 2 | -. 479 | . 427 | . 767 | 189 |
| $\mathrm{C}_{4}$ | 1 | - . 739 | . 054 | -. 672 | . 200 |  | 3 | . 676 | . 737 | . 012 | 245 |
|  | 2 | -. 647 | 220 | 730 | . 210 | $\mathrm{C}_{14}$ | 1 | - . 142 | . 124 | -. 982 | . 174 |
|  | 3 | . 188 | 974 | -. 128 | 247 |  | 2 | -. 604 | . 775 | . 185 | 207 |
| C | 1 | -. 104 | . 059 | -. 993 | 200 |  | 3 | . 784 | . 620 | -. 035 | 283 |
|  | 2 | -. 917 | . 382 | . 119 | 238 | $\mathrm{C}_{15}$ | 1 | . 111 | . 175 | -. 978 | 167 |
|  | 3 | . 386 | . 922 | . 015 | . 257 |  | 2 | -. 173 | . 973 | . 154 | . 233 |
| $\mathrm{C}_{6}$ | 1 | -. 439 | . 022 | 898 | . 183 |  | 3 | . 979 | . 152 | . 138 | . 281 |

of each oxygen atom parallel to the $\mathrm{C}-\mathrm{O}$ bond would be increased by a distribution between longer and shorter $\mathrm{C}-\mathrm{O}$ bonds of the asymmetric molecule.

The asymmetric environment of the oxygen atoms, as seen from Fig. 4, would lead one to expect asymmetry of the two carbonyl groups. But the symmetry of the two halves of the molecule in both positional and thermal parameters is quite good. Since this symmetry persists even though the two halves of the molecule do not have a symmetry environment, this is good evidence that the molecular symmetry is real, and that the hydrogen bond is symmetric although probably not linear. Of course, this structure does not preclude the possibility that the hydrogen distribution is split into two in a symmetrical double well.

A comparison was made between the packing efficiencies of the nonisostructural compounds bis- $(m$ -chlorobenzoyl)-methane and bis-( $m$-bromobenzoyl)methane. The packing coefficient of Kitaigorodskii ${ }^{9}$
was calculated for each of the compounds. This packing coefficient represents the ratio of the volume of the unit cell occupied by the molecules in the unit cell to the volume of the unit cell. The coefficient of the bromo derivative was 0.686 and that of the chloro derivative was 0.691 . If the chloro derivative were assumed to be isostructural with the bromo derivative, the packing coefficient would be 0.648 . The unit cell volume of the bromo compound is $87 \AA \AA^{3}$ larger than the chloro compound while only $53 \AA .^{3}$ would be required for bromine instead of chlorine atoms. Evidently the chloro derivative packs more efficiently than the bromo derivative. The bromine atoms in bis-( $m$-bromobenzoyl)-methane tend to pack in sheets while the chlorine atoms in bis- ( $m$-chlorobenzoyl)methane tend to pack in zig-zag chains. The large congregation of bromine atoms may in some way compensate for the loss in packing efficiency.
(9) A. Kitaigorodskii, '•Organic Chemical Crystallography,'" Consultants Bureau, New York, N. Y., 1955.

## [Contribution from the Department of Chemistry, the Johns Hopkins University, Baltimore 18, Md.]

# The Fragmentation of Some Boron Hydrides by Electron Impact ${ }^{1}$ 

By T. P. Fehlner and W. S. Koski<br>Received August 12, 1963


#### Abstract

The fragmentation of isotopically labeled volatile boron hydrides by electron impact has been studied. Monoisotopic spectra, appearance potentials of selected fragments, and metastable transitions are reported both for protonated and deuterated compounds. Ionization potentials are given for diborane, tetraborane, penta-borane-9 and -11, and hexaborane. Heats of formation are calculated for the various fragment ions produced and are used in determining the decomposition paths for the parent ions. Structures of several fragment ions are postulated from data on isotopically labeled hydrides; ionization potentials are calculated from the corresponding appearance potentials.


## Introduction

In a previous paper the fragmentation of tetraborane was studied utilizing measured appearance potentials and the observed metastable transitions in the spectra
of monoisotopic and isotopically labeled tetraboranes. ${ }^{2}$ Since then, this approach has been extended to the rest

[^2] Energy Commission.
(2) T. P. Fehlner and W. S. Koski, J. Am. Chem. Soc., 85, 1905 (1963).


[^0]:    (1) (a) Taken in part from a thesis by Gordon Engebretson submitted November 7. 1962, to Iowa State University. Ames. Iowa, in partial fulfillment of the requirements for the Ph.D. degree. This work was parformed under contract with the Atomic Energy Commission. (b) Deceased. October 9.1963.

[^1]:    (3) W. Borduin. M.S. Thesis, Iowa State University Library. 1956.
    (4) (a) D. Williams, Iowa State University. unpublished: (b) W. Busing and H. Levy, Acta Cryst.. 10, 180 (1957).
    (5) W. Hamilton. ibid., 8, 185 (1955).

[^2]:    (1) This work was done under the auspices of the United States Atomic

